

- ▶ ILYA SHAPIROVSKY, *Satisfiability problems on sums of Kripke frames*.  
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The complexity of satisfiability problems in modal logic has been systematically investigated since the 1970s; for many logics (e.g, for the standard systems K, T, K4, S4) this problem is known to be PSPACE-complete [1], [3].

In many cases, PSPACE upper bound can be established using the operation of sum of relational structures (Kripke frames) [2]. Given a family  $(F_i \mid i \text{ in } I)$  of frames indexed by elements of another frame  $I$  (of the same signature), the *sum of the frames  $F_i$ 's over  $I$*  is obtained from their disjoint union by connecting elements of  $i$ -th and  $j$ -th distinct components according to the relations in  $I$ . Given a class  $\mathcal{F}$  of frames-summands and a class  $\mathcal{I}$  of frames-indices,  $\sum_{\mathcal{I}} \mathcal{F}$  denotes the class of all sums of  $F_i$ 's in  $\mathcal{F}$  over  $I$  in  $\mathcal{I}$ . In this talk we discuss conditions under which the modal satisfiability problem on  $\sum_{\mathcal{I}} \mathcal{F}$  is polynomial space Turing reducible to the modal satisfiability problem on  $\mathcal{F}$ .

[1] R. LADNER, *The computational complexity of provability in systems of modal propositional logic*, **SIAM Journal on Computing**, vol. 6 (1977), no. 3, pp. 467–480.

[2] I. SHAPIROVSKY, *PSPACE-decidability of Japaridze's polymodal logic*, **Advances in modal logic** (London), AiML, vol. 7, College Publications, 2008, pp. 289–304.

[3] E. SPAAN, **Complexity of modal logics**, PhD thesis, University of Amsterdam, Institute for Logic, Language and Computation, 1993.