

- MANAT MUSTAFA, SERGEY OSPICHEV, *About Rogers semilattices of finite families in Ershov hierarchy.*

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There is a well-known result, that any finite family of c.e. sets has computable principal numbering [1]. In [2], K. Abeshev shows that there is a finite family of sets in Ershov hierarchy without  $\Sigma_2^{-1}$ -computable principal numbering. With the help of  $\Gamma$ -operator in [3], above result can be generalized to any level (finite and successor ordinals) of Ershov hierarchy. Here we concentrate our interest to different types of  $\Sigma_2^{-1}$ -computable numberings of finite families of  $\Sigma_2^{-1}$ -sets and c.e.-sets. The main result is:

**Theorem.** *Let  $\mathcal{S} = \{A, B\}$  be any family with  $A, B$  are c.e. sets with  $A \subseteq B$  but  $A \setminus B$  is not c.e., then the Rogers semilattice  $\mathcal{R}_2^{-1}(\mathcal{S})$  is isomorphic to family  $L_0^m$  of all  $m$ -degrees of c.e. sets.*

**Corollary.** *Any  $\Sigma_2^{-1}$ -computable numbering of  $\mathcal{S}$  is equivalent to some computable numbering of  $\mathcal{S}$ .*

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[1] A. H. LACHLAN, *Standard classes of recursively enumerable sets*, **Z. Math. Log. Grundle. Math.** vol. 10 (1964), no. 2-3, pp. 23–42.

[2] K. ABESHEV, *On the existence of universal numberings for finite families of d.c.e. sets*, **Mathematical Logic Quarterly**, vol. 60 (2014), no. 3, pp. 161–167.

[3] I. HERBERT, S. JAIN, S. LEMPP, M. MUSTAFA, F. STEPHAN, *Reductions between types of numberings*, **Preprint**, [www.math.wisc.edu/~lempp/papers/redandnumb.pdf](http://www.math.wisc.edu/~lempp/papers/redandnumb.pdf).